2.2

Essential Question What does it mean when a whole number is multiplied by a fraction? Will the product be *greater than* or *less than* the whole number?

EXAMPLE: Multiplying a Fraction and a Whole Number

You have 3 gallons of paint. You use $\frac{3}{4}$ of the paint. How many gallons did you use?

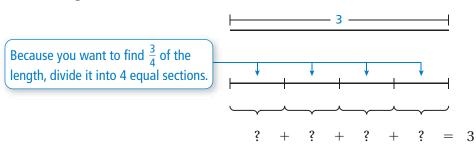
THINK ABOUT THE QUESTION: One way to think about this question is to rewrite the question.

Words: What is $\frac{3}{4}$ of 3?

Numbers:
$$\frac{3}{4} \times 3 = ?$$

Here is one way to get the answer.

• **Draw** a length of 3.



Now, you need to think of a way to divide 3 into 4 equal parts.

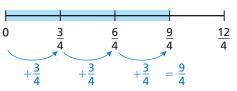
• **Rewrite** the number 3 as a fraction whose numerator is divisible by 4.

In this form, you see that $\frac{12}{4}$ can be divided into four equal parts of $\frac{3}{4}$.

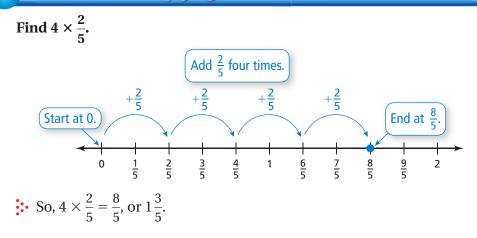
• Each part is $\frac{3}{4}$ gallon and you used three of them. Written as multiplication, you have

$$\frac{3}{4} \times 3 = \frac{9}{4}.$$

So, you used $\frac{9}{4}$ gallons of paint.



EXAMPLE: Multiplying a Whole Number and a Fraction



Inductive Reasoning

Work with a partner. Complete the table using a number line.

	Exercise	Repeated Addition
1	3. $\frac{3}{4} \times 3$	$\frac{3}{4} + \frac{3}{4} + \frac{3}{4} = \frac{9}{4}$
2	4. $4 \times \frac{2}{5}$	$\frac{2}{5} + \frac{2}{5} + \frac{2}{5} + \frac{2}{5} = \frac{8}{5}$
	5. $\frac{7}{6} \times 5$	
	6. $3 \times \frac{9}{5}$	
	7. $\frac{1}{3} \times 12$	

What Is Your Answer?

- 8. a. Write a real-life problem that is related to the product $\frac{2}{3} \times 5$.
 - **b.** Write a different real-life problem that is related to the product $5 \times \frac{2}{3}$.
 - **c.** Are the two products equal? How is your answer related to the Commutative Property of Multiplication?
- **9. IN YOUR OWN WORDS** What does it mean when a whole number is multiplied by a fraction? Will the product be *greater than* or *less than* the whole number?
- **10.** Write a general rule for multiplying fractions and whole numbers.

Practice

Use what you learned about multiplying fractions and whole numbers to complete Exercises 4–11 on page 54.

2.2 Lesson



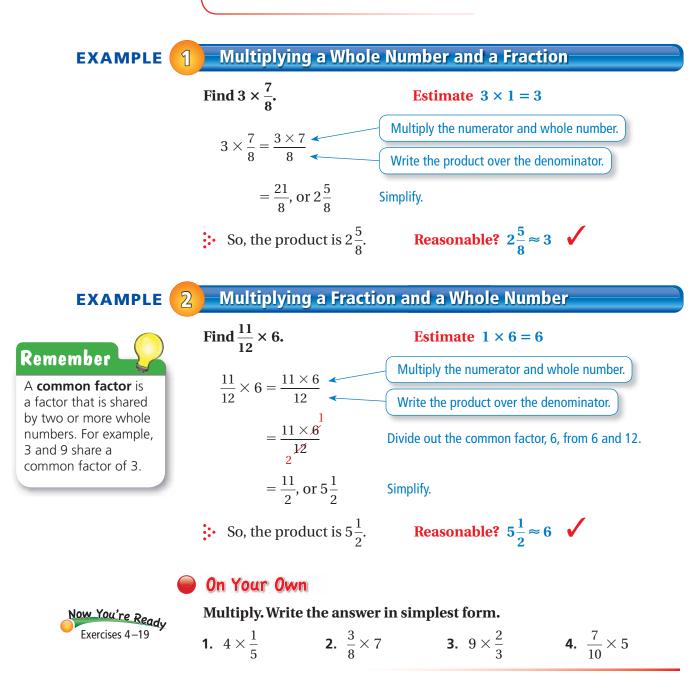


Multiplying Fractions and Whole Numbers

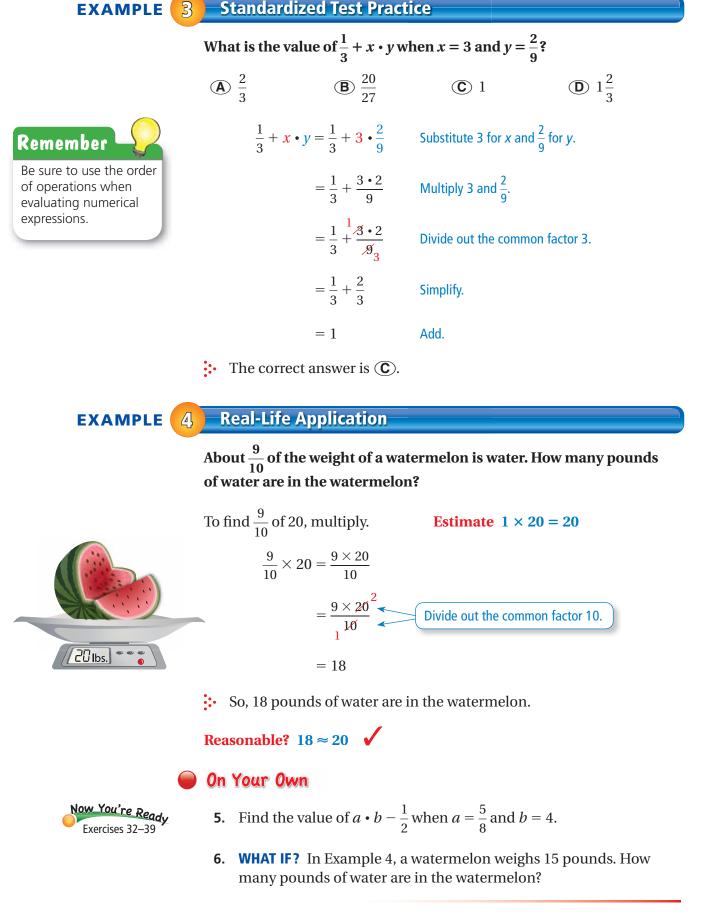
Words Multiply the numerator of the fraction by the whole number. Then write the product over the denominator.

Numbers
$$2 \times \frac{4}{9} = \frac{2 \times 4}{9} = \frac{8}{9}$$

Algebra $a \cdot \frac{b}{c} = \frac{a \cdot b}{c}$, where $c \neq 0$



EXAMPLE



2.2 Exercises



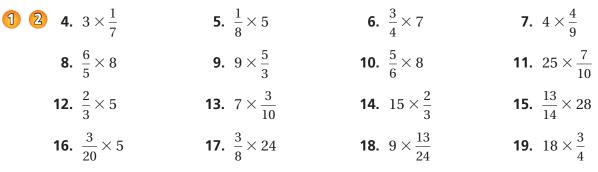


Vocabulary and Concept Check

- 1. WRITING Describe how to multiply a fraction by a whole number.
- **2.** NUMBER SENSE Use repeated addition to find the product $6 \times \frac{7}{9}$.
- **3.** NUMBER SENSE Without multiplying, which is greater, $\frac{1}{3} \times 24$ or $\frac{1}{4} \times 24$? Explain.



Multiply. Write the answer in simplest form.



ERROR ANALYSIS Describe and correct the error in finding the product.



- **22.** CDs Your friend has 12 CDs and $\frac{3}{4}$ of them are pop music. How many CDs are pop music?
- **23. OATMEAL MUFFINS** A batch of oatmeal muffins calls for $\frac{2}{3}$ cup of oats. How many cups of oats do you need to make four batches of muffins?
- **24.** RAIN There are 365 days in a year and rain falls on $\frac{2}{5}$ of the days. How many days does it rain during the year?

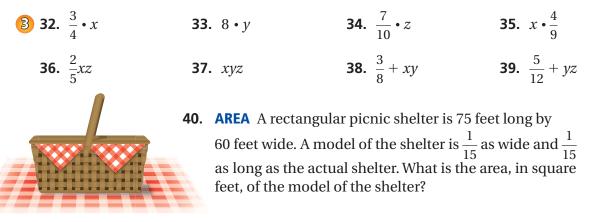
Use compatible numbers to estimate the product.

25.
$$\frac{1}{3} \times 17$$
 26. $35 \times \frac{1}{8}$ **27.** $22 \times \frac{5}{6}$ **28.** $\frac{4}{5} \times 7$

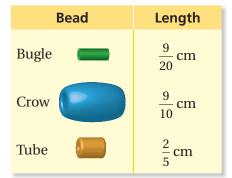
Tell how the Commutative and Associative Properties of Multiplication can help find the product mentally. Then find the product.

29. $25 \times 6 \times \frac{2}{5}$ **30.** $\left(8 \times \frac{5}{9}\right) \times 18$ **31.** $\frac{3}{7} \times 13 \times 14$

ALGEBRA Evaluate the expression when x = 6, $y = \frac{3}{16}$, and z = 20.



- **41. REASONING** You spend $\frac{1}{3}$ of your money and your friend spends $\frac{1}{2}$ of her money shopping. Is it possible that you spend more money than your friend? Explain your reasoning.
- **42. NECKLACES** You make bead necklaces using the beads shown in the table. Each necklace has a clasp that is $\frac{9}{10}$ centimeter long.
 - **a.** How long is a necklace with 48 bugle beads and 24 tube beads?
 - **b.** How long is a necklace with 18 bugle beads, 18 crow beads, and 18 tube beads?



c. Reasoning: You want to make a necklace 38 centimeters or longer. You have 26 bugle beads, 18 crow beads, and 16 tube beads. Do you have enough beads? If not, what is the smallest number of bugle beads you need to add to make the necklace? Explain how you found your answer.

A		Fair Gam	e Review what y	you learned in previous gr	ades & lessons	
Evaluate the expression.						
	43.	$\frac{3\times 5}{2\times 4}$	44. $\frac{9 \times 2}{1 \times 5}$	45. $\frac{4 \times 8}{7 \times 25}$	46. $\frac{10 \times 13}{3 \times 11}$	
	47. MULTIPLE CHOICE What is the area of a parallelogram with a base of 12 inches and a height of 4 inches?					
		A 24 in.	B 48 in.	(C) 24 in.^2	(D) 48 in.^2	