## 2.6 Dividing Mixed Numbers

## Essential Question How can you use division



by a mixed number as part of a story?

### **EXAMPLE:** Writing a Story

Write a story that uses the division problem  $6 \div 1\frac{1}{2}$ . Draw pictures for your story.

#### There are many possible stories. Here is one about a camping trip.

Joe goes on a camping trip with his aunt, his uncle, and three cousins. They leave at 5:00 P.M. and drive 2 hours to the campground.





Joe helps his uncle put up three tents. His aunt cooks hamburgers on a grill that is over a fire.

In the morning, Joe tells his aunt that he is making pancakes for everyone. He decides to triple the recipe so there will be plenty of pancakes for everyone. A single recipe uses 2 cups of water, so he needs a total of 6 cups.





Joe's aunt has a 1-cup measuring cup and a <sup>1</sup>/<sub>2</sub>-cup measuring cup. The water faucet is about 50 yards from the campsite. Joe tells his cousins that he can get 6 cups of water in only 4 trips.

When his cousins ask him how he knows that, he uses a stick to draw a diagram in the dirt. Joe says "This diagram shows that there are four  $1\frac{1}{2}$ 's in 6." In other words,





#### **EXAMPLE:** Dividing by a Mixed Number

Show how Joe solves the division problem in Example 1.



#### ACTIVITY: Writing a Story

Work with a partner. Think of a story that uses division by a mixed number.



- a. Write your story. Then draw pictures for your story.
- **b.** Solve the division problem and use the answer in your story. Include a diagram of the division problem.

### -What Is Your Answer?

**4. IN YOUR OWN WORDS** How can you use division by a mixed number as part of a story?

In Example 1, the units of the answer are trips.

$$Cups \div \frac{Cups}{Trips} = Cups \times \frac{Trips}{Cups}$$

Practice

$$= \text{Cups} \times \frac{\text{Trips}}{\text{Cups}} = \text{Trips}$$

#### Find the units for the following division problems.

5. Miles  $\div \frac{\text{Miles}}{\text{Hour}}$ 6. Dollars  $\div \frac{\text{Dollars}}{\text{Hour}}$ 7. Miles  $\div$  Hour8. Dollars  $\div$  Hour

Use what you learned about dividing mixed numbers to complete Exercises 5–12 on page 82.





#### **Dividing Mixed Numbers**

Write each mixed number as an improper fraction. Then divide as you would with proper fractions.



**1.**  $1\frac{3}{7} \div \frac{2}{3}$  **2.**  $2\frac{1}{6} \div \frac{3}{4}$  **3.**  $8\frac{1}{4} \div 1\frac{1}{2}$  **4.**  $6\frac{4}{5} \div 2\frac{1}{8}$ 

EXAMPLE	3 Using Order of Operations		
	Evaluate $5\frac{1}{4} \div 1\frac{1}{8} - \frac{2}{3}$ .		
Remember Be sure to check your answers whenever possible. In Example 3, you can use estimation to check that your answer is reasonable. $5\frac{1}{4} \div 1\frac{1}{8} - \frac{2}{3}$ $\approx 5 \div 1 - 1$ = 5 - 1 = 4	$5\frac{1}{4} \div 1\frac{1}{8} - \frac{2}{3} = \frac{21}{4} \div \frac{9}{8} - \frac{2}{3}$	Write each mixed number as an improper fraction.	
	$=\frac{21}{4}\times\frac{8}{9}-\frac{2}{3}$	Multiply by the reciprocal of $\frac{9}{8}$ , which is $\frac{8}{9}$ .	
	$=\frac{7}{1}\frac{21\times8}{4\times9}^{2}-\frac{2}{3}$	Multiply $\frac{21}{4}$ and $\frac{8}{9}$ . Divide out common factors.	
	$=\frac{14}{3}-\frac{2}{3}$	Simplify.	
	$=\frac{12}{3}$ , or 4	Subtract.	

**Real-Life Application EXAMPLE** A

> One serving of tortilla soup is  $1\frac{2}{3}$  cups. A restaurant cook makes 50 cups of soup. Is there enough to serve 35 people? Explain.

Divide 50 by  $1\frac{2}{3}$  to find the number of available servings.



Exercises 29-37

Rewrite each number as an improper fraction.  $= \frac{50}{1} \cdot \frac{3}{5}$  Multiply by the reciprocal of  $\frac{5}{3}$ , which is  $\frac{3}{5}$ .

Multiply fractions. Divide out common factors.

Simplify.

No. Because 30 is less than 35, there is not enough soup to serve 35 people.

### **On Your Own**

Evaluate the expression.

- 5.  $1\frac{1}{2} \div \frac{1}{6} \frac{7}{8}$ **6.**  $3\frac{1}{3} \div \frac{5}{6} + \frac{8}{9}$ 7.  $\frac{2}{5} + 2\frac{4}{5} \div 1\frac{3}{4}$ 8.  $\frac{2}{3} - 1\frac{4}{7} \div 4\frac{5}{7}$
- 9. In Example 4, can 30 cups of tortilla soup serve 15 people? Explain.

### 2.6 Exercises

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- **1. VOCABULARY** What is the reciprocal of  $7\frac{1}{3}$ ?
- **2.** NUMBER SENSE Is  $5\frac{1}{4} \div 3\frac{1}{2}$  the same as  $3\frac{1}{2} \div 5\frac{1}{4}$ ? Explain.
- **3. NUMBER SENSE** Is the reciprocal of an improper fraction *sometimes, always,* or *never* a proper fraction? Explain.
- 4. DIFFERENT WORDS, SAME QUESTION Which is different? Find "both" answers.

What is  $5\frac{1}{2}$  divided by  $\frac{1}{8}$ ?Find the quotient of  $5\frac{1}{2}$  and  $\frac{1}{8}$ .What is  $5\frac{1}{2}$  times 8?Find the product of  $5\frac{1}{2}$  and  $\frac{1}{8}$ .

## S Practice and Problem Solving

Divide. Write the answer in simplest form.

<b>2 5.</b> $2\frac{1}{4} \div \frac{3}{4}$	<b>6.</b> $3\frac{4}{5} \div \frac{2}{5}$	<b>7.</b> $8\frac{1}{8} \div \frac{5}{6}$	<b>8.</b> $7\frac{5}{9} \div \frac{4}{7}$
<b>9.</b> $7\frac{1}{2} \div 1\frac{9}{10}$	<b>10.</b> $3\frac{3}{4} \div 2\frac{1}{12}$	<b>11.</b> $7\frac{1}{5} \div 8$	<b>12.</b> $8\frac{4}{7} \div 15$
<b>13.</b> $8\frac{1}{3} \div \frac{2}{3}$	<b>14.</b> $9\frac{1}{6} \div \frac{5}{6}$	<b>15.</b> $13 \div 10 \frac{5}{6}$	<b>16.</b> $12 \div 5\frac{9}{11}$
<b>17.</b> $\frac{7}{8} \div 3\frac{1}{16}$	<b>18.</b> $\frac{4}{9} \div 1\frac{7}{15}$	<b>19.</b> $4\frac{5}{16} \div 3\frac{3}{8}$	<b>20.</b> $6\frac{2}{9} \div 5\frac{5}{6}$

21. ERROR ANALYSIS Describe and correct the error in finding the quotient.

 $X \quad 3\frac{1}{2} \div 1\frac{2}{3} = 3\frac{1}{2} \times 1\frac{3}{2} = \frac{7}{2} \times \frac{5}{2} = \frac{35}{4} = 8\frac{3}{4}$ 

- **22. DOG FOOD** A bag contains 42 cups of dog food. Your dog eats  $2\frac{1}{3}$  cups of dog food each day. How many days does the bag of dog food last?
- **23.** HAMBURGERS How many  $\frac{1}{4}$ -pound hamburgers can be made from  $3\frac{1}{2}$  pounds of ground beef?
- **24.** BOOKS How many  $1\frac{3}{5}$ -inch thick books can fit on a  $14\frac{1}{2}$ -inch long bookshelf?

**Evaluate the expression.** 

**3 29.**  $5\frac{5}{6} \div 3\frac{3}{4} - \frac{2}{9}$ **30.**  $6\frac{1}{2} - \frac{7}{8} \div 5\frac{11}{16}$ **31.**  $9\frac{1}{6} \div 5 + 3\frac{1}{3}$ **33.**  $\frac{3}{5} \times \frac{7}{12} \div 2\frac{7}{10}$  **34.**  $4\frac{3}{8} \div \frac{3}{4} \times \frac{4}{7}$ **32.**  $3\frac{3}{5} + 4\frac{4}{15} \div \frac{4}{9}$ **35.**  $1\frac{9}{11} \times 4\frac{7}{12} \div \frac{2}{3}$ **36.**  $3\frac{4}{15} \div \left(8 \times 6\frac{3}{10}\right)$  **37.**  $2\frac{5}{14} \div \left(2\frac{5}{8} \times 1\frac{3}{7}\right)$ 

**38.** TRAIL MIX You have 12 cups of granola and  $8\frac{1}{2}$  cups of peanuts to make trail mix. What is the greatest number of full batches of trail mix you can make? Explain how you found your answer.

Trail Mix  $2\frac{3}{4}$  cups granola  $1\frac{1}{3}$  cups peanuts



- **39. RAMPS** You make skateboard ramps by cutting pieces from a board that is  $12\frac{1}{2}$  feet long.
  - a. Estimate how many ramps you can cut from the board. Is your estimate reasonable? Explain.
  - **b.** How many ramps can you cut from the board? How much wood is left over?
- Reasoning At a track meet, the longest shot put throw by a boy is 40. 25 feet and 8 inches. The longest shot put throw by a girl is 19 feet and 3 inches. How many times greater is the longest shot put throw by a boy than by a girl?

# Fair Game Review What you learned in previous grades & lessons

#### Write the number as a decimal.

- 41. forty-three hundredths **42.** thirteen thousandths
- **43.** three and eight tenths 44. seven and nine thousandths
- **45.** MULTIPLE CHOICE The winner in a vote for class president received  $\frac{3}{4}$  of the 240 votes. How many votes did the winner receive?

**(A)** 60 **(B)** 150 **(C)** 180 **(D)** 320