### 4.1 The Percent Equation

Essential Question How can you use modest ostimate percent questions?
(1) ACIIVIJY: Estimating a Percent

Work with a partner. Estimate the locations of $50 \%, 75 \%, 40 \%, 6 \%$, and $65 \%$ on the model. $50 \%$ is done for you.


## 2 ACTIVIIY: Estimating a Part of a Number

The statement " $25 \%$ of 12 is 3 " has three numbers. In real-life problems, any one of these numbers can be unknown.


Which number
is missing?
3
25\%
12

Question
What is $\mathbf{2 5 \%}$ of $\mathbf{1 2}$ ?
3 is what percent of 12 ?
3 is $25 \%$ of what?

Type of Question
Find a part of a number.
Find a percent.
Find the whole.

Work with a partner. Estimate the answer to each question using a model.
a. Sample: What number is $50 \%$ of 30 ?

$\because$ So, from the model, 15 is $50 \%$ of 30 .
b. What number is $75 \%$ of 30 ?
c. What number is $40 \%$ of 30 ?
d. What number is $6 \%$ of 30 ?
e. What number is $65 \%$ of 30 ?

## 3 ACIIVITY: Estimating a Percent

Work with a partner. Estimate the answer to the question using a model.

a. Sample: 15 is what percent of 75 ?

$\therefore \cdot$ So, 15 is $20 \%$ of 75 .
b. 5 is what percent of 20 ?
c. 18 is what percent of 40 ?
d. 50 is what percent of 80 ?
e. 75 is what percent of 50 ?

## 4 ACTIVIJY: Estimating a Whole

Work with a partner. Estimate the answer to the question using a model.

a. Sample: 24 is $33 \frac{1}{3} \%$ of what number?

$\therefore$ So, 24 is $33 \frac{1}{3} \%$ of 72 .
b. 13 is $25 \%$ of what number?
c. 110 is $20 \%$ of what number?
d. 75 is $75 \%$ of what number?
e. 81 is $45 \%$ of what number?

## What Is Your Answer?

5. IN YOUR OWN WORDS How can you use models to estimate percent questions? Give examples to support your answer.

## Key Vocabulary

percent, p. 160

A percent is a ratio whose denominator is 100 . Here are two examples.

$$
4 \%=\frac{4}{100}=0.04 \quad 25 \%=\frac{25}{100}=0.25
$$

## Key Idea

## The Percent Equation

Words To represent " $a$ is $p$ percent of $w$," use an equation.


## EXAMPLE <br> (7) Finding a Part of a Number

What number is $\mathbf{2 4 \%}$ of 50 ?


## Common Error

Remember to convert a percent to a fraction or decimal before using the percent equation. For Example 1, write $24 \%$ as $\frac{24}{100}$.

$$
\begin{aligned}
a & =p \cdot w & & \text { Write percent equation. } \\
& =\frac{24}{100} \cdot 50 & & \text { Substitute } \frac{24}{100} \text { for } p \text { and } 50 \text { for } w . \\
& =12 & & \text { Multiply. }
\end{aligned}
$$

$\therefore$ So, 12 is $24 \%$ of 50 .
Reasonable? $12 \approx 12.5$

EXAMPLE 2 finding a percent
9.5 is what percent of 25 ?


$$
\begin{aligned}
a & =p \cdot w & & \text { Write percent equation. } \\
9.5 & =p \cdot 25 & & \text { Substitute } 9.5 \text { for } a \text { and } 25 \text { for } w . \\
0.38 & =p & & \text { Divide each side by } 25 .
\end{aligned}
$$

$\therefore$ Because 0.38 equals $38 \%, \quad$ Reasonable? $38 \% \approx 40 \%$ 9.5 is $38 \%$ of 25 .

39 is $52 \%$ of what number?


$$
\begin{aligned}
a & =p \cdot w \\
39 & =0.52 \cdot w
\end{aligned}
$$

$$
75=w \quad \text { Divide each side by } 0.52
$$

$\because$ So, 39 is $52 \%$ of 75 .
Reasonable? $75 \approx 78$

## On Your Own

Exercises 10-17

Write and solve an equation to answer the question.

1. What number is $10 \%$ of 20 ?
2. What number is $150 \%$ of 40 ?
3. 3 is what percent of 600 ?
4. 18 is what percent of 20 ?
5. 8 is $80 \%$ of what number?
6. 90 is $18 \%$ of what number?

## EXAMPLE

## 4 Rea-Life Application

## 8th Street Cafe

Date: May04’10 05:45PM
Table: 29
Server: Charity
Food Total 27.50

Tax
Subtotal 1.65

Tip: $\qquad$
TOTAL: $\qquad$
Thank You
a. Find the percent of sales tax on the food total.
b. Find the amount of a $16 \%$ tip on the food total.
a. Answer the question: $\$ 1.65$ is what percent of $\$ 27.50$ ?

$$
\begin{aligned}
a & =p \cdot w & & \text { Write percent equation. } \\
1.65 & =p \cdot 27.50 & & \text { Substitute } 1.65 \text { for } a \text { and } 27.50 \text { for } w . \\
0.06 & =p & & \text { Divide each side by } 27.50 .
\end{aligned}
$$

$\therefore$ Because 0.06 equals $6 \%$, the percent of sales tax is $6 \%$.
b. Answer the question: What tip amount is $16 \%$ of $\$ 27.50$ ?

$$
\begin{aligned}
a & =p \cdot w & & \text { Write percent equation. } \\
& =0.16 \cdot 27.50 & & \text { Substitute } 0.16 \text { for } p \text { and } 27.50 \text { for } w . \\
& =4.40 & & \text { Multiply. }
\end{aligned}
$$

$\therefore$ So, the amount of the tip is $\$ 4.40$.

## On Your Own

7. WHAT IF? In Example 4, find the amount of a $20 \%$ tip on the food total.

## 4.1 <br> Exercises

## Vocabulary and Concept Check

1. VOCABULARY Write the percent equation in words.
2. REASONING A number $n$ is $150 \%$ of number $m$. Is $n$ greater than, less than, or equal to $m$ ? Explain your reasoning.
3. DIFFERENT WORDS, SAME QUESTION Which is different? Find "both" answers.

What number is $20 \%$ of 55 ?
$20 \%$ of 55 is what number?

55 is $20 \%$ of what number?
$0.2 \cdot 55$ is what number?

## Practice and Problem Solving

Estimate the answer to the question using a model.
4. What number is $24 \%$ of 80 ?
6. 15 is $30 \%$ of what number?
8. 20 is what percent of 52 ?

## Write and solve an equation to answer the question.

10. $20 \%$ of 150 is what number?
11. 45 is what percent of 60 ?
12. $35 \%$ of what number is 35 ?
13. $32 \%$ of 25 is what number?
14. 29 is what percent of 20 ?
15. $0.5 \%$ of what number is 12 ?
16. What percent of 300 is 51 ?
17. $120 \%$ of what number is 102 ?
18. 15 is what percent of 40 ?
19. What number is $120 \%$ of 70 ?
20. 48 is $75 \%$ of what number?

ERROR ANALYSIS Describe and correct the error in using the percent equation.
18. What number is $35 \%$ of 20 ?

$$
\begin{aligned}
a & =p \cdot w \\
& =35 \cdot 20 \\
& =700
\end{aligned}
$$

PUZZLE There were $w$ signers of the Declaration of Independence. The youngest was Edward Rutledge, who was $x$ years old. The oldest was Benjamin Franklin, who was $y$ years old.
23. $x$ is $25 \%$ of 104 . What was Rutledge's age?
24. 7 is $10 \%$ of $y$. What was Franklin's age?
25. $w$ is $80 \%$ of $y$. How many signers were there?
26. $y$ is what percent of $(w+y-x)$ ?

27. REASONING How can you tell whether the percent of a number will be greater than, less than, or equal to the number?
28. SURVEY In a survey, a group of students were asked their favorite sport. "Other" sports were chosen by 18 people.
a. How many students participated?
b. How many chose football?
29. WATER TANK Water tank $A$ has a capacity of 550 gallons and is $66 \%$ full. Water $\operatorname{tank} B$ is $53 \%$ full. The ratio of the capacity of $\operatorname{tank} A$ to $\operatorname{tank} B$ is $11: 15$.
a. How much water is in $\operatorname{tank} A$ ?
b. What is the capacity of $\operatorname{tank} B$ ?
c. How much water is in tank $B$ ?
30. TRUE OR FALSE? Tell whether the statement is true or false. Explain your reasoning.

If $W$ is $25 \%$ of $Z$, then $Z: W$ is $75: 25$.
31. 子Reasoning The table shows your test results for math class. What test score is needed on the last exam to earn $90 \%$ of the total points?

| Test Score | Point Value |
| :---: | :---: |
| $83 \%$ | 100 |
| $91.6 \%$ | 250 |
| $88 \%$ | 150 |
| $?$ | 300 |

## Fair Game Review what you learned in previous grades \& lessons

Simplify. Write as a decimal. SKILLS REVIEW HANDBOOK
32. $\frac{10-4}{10}$
33. $\frac{25-3}{25}$
34. $\frac{105-84}{84}$
35. $\frac{170-125}{125}$
36. MULTIPLE CHOICE There are 160 people in a grade. The ratio of boys to girls is 3 to 5 . Which proportion can you use to find the number $x$ of boys?

SECTION 3.4
(A) $\frac{3}{8}=\frac{x}{160}$
(B) $\frac{3}{5}=\frac{x}{160}$
(C) $\frac{5}{8}=\frac{x}{160}$
(D) $\frac{3}{5}=\frac{160}{x}$

